

1. Solve algebraically the simultaneous equations

$$\begin{aligned}
 & x^2 + y^2 = 25 \\
 & y = 2x + 5 \quad | \text{Sub } y = 2x + 5 \text{ into } x^2 + y^2 = 25 \\
 & x^2 + (2x+5)^2 = 25 \\
 & x^2 + (2x+5)(2x+5) = 25 \\
 & x^2 + 4x^2 + 10x + 10x + 25 = 25 \\
 & 5x^2 + 20x + 25 = 25 \\
 & 5x^2 + 20x = 0 \\
 & x^2 + 4x = 0 \quad | \text{Factorize} \\
 & x(x + 4) = 0 \quad | \text{Set each factor to zero} \\
 & x=0 \quad | \text{Solutions for } x \\
 & x+4=0 \quad | \text{Solutions for } x \\
 & x=-4 \quad | \text{Solutions for } x
 \end{aligned}$$

$$\begin{aligned}
 & x^2 + y^2 = 25 \\
 & y - 2x = 5 \\
 & y = 2x + 5 \\
 & y - 2x = 5 \\
 & \text{Sub } x=0 \\
 & y - 2(0) = 5 \\
 & y = 5 \\
 & \text{Sub } x=-4 \\
 & y - 2(-4) = 5 \\
 & y + 8 = 5 \\
 & y = -3
 \end{aligned}$$

$x=0, y=5$ and $x=-4, y=-3$

2. Solve algebraically the simultaneous equations

$$\begin{aligned}x^2 + y^2 &= 25 \\y - 3x &= 13\end{aligned}$$

$$y - 3x = 13. \quad y = 13 + 3x \quad (1)$$

$$x^2 + y^2 = 25. \quad x^2 + (13 + 3x)^2 = 25$$

$$x^2 + (13 + 3x)(13 + 3x) = 25. \quad x^2 + 169 + 39x + 39x + 9x^2$$

$$= 10x^2 + 78x + 169 = 25. \quad 10x^2 + 78x + 144 = 0. \quad (1)$$

$$(5x + 24)(x + 3) = 0.$$

$$5x + 24 = 0. \quad x + 3 = 0.$$

$$5x = -24$$

$$x = -\frac{24}{5}. \quad (1)$$

when $x = -\frac{24}{5}$:

$$y = 13 + 3\left(-\frac{24}{5}\right) = -\frac{7}{5}$$

when $x = -3$:

$$y = 13 + 3(-3) = y = 4 \quad (1)$$

$$\begin{aligned}x &= -\frac{24}{5}, \quad y = -\frac{7}{5} \\x &= -3, \quad y = 4.\end{aligned}$$

3. Solve the simultaneous equations

$$\begin{array}{l} \textcircled{1} \quad 3x + y = -4 \\ \textcircled{2} \quad 3x - 4y = 6 \end{array}$$

$y = -4 - 3x$

$$\textcircled{2} \quad 3x - 4y = 6$$

$$3x - 4(-4 - 3x) = 6$$

$$3x + 16 + 12x = 6$$

$$15x + 16 = 6 \quad) -16$$

$$15x = -10 \quad) \div 15$$

$$x = -\frac{10}{15} \quad \textcircled{1}$$

$$\textcircled{1} \quad 3x + y = -4$$

$$y = -4 - 3x$$

$$y = -4 - 3\left(-\frac{10}{15}\right)$$

$$y = -4 + \frac{30}{15}$$

$$y = -4 + 2$$

$$y = -2. \quad \textcircled{1}$$

$$x = -\frac{2}{3}$$

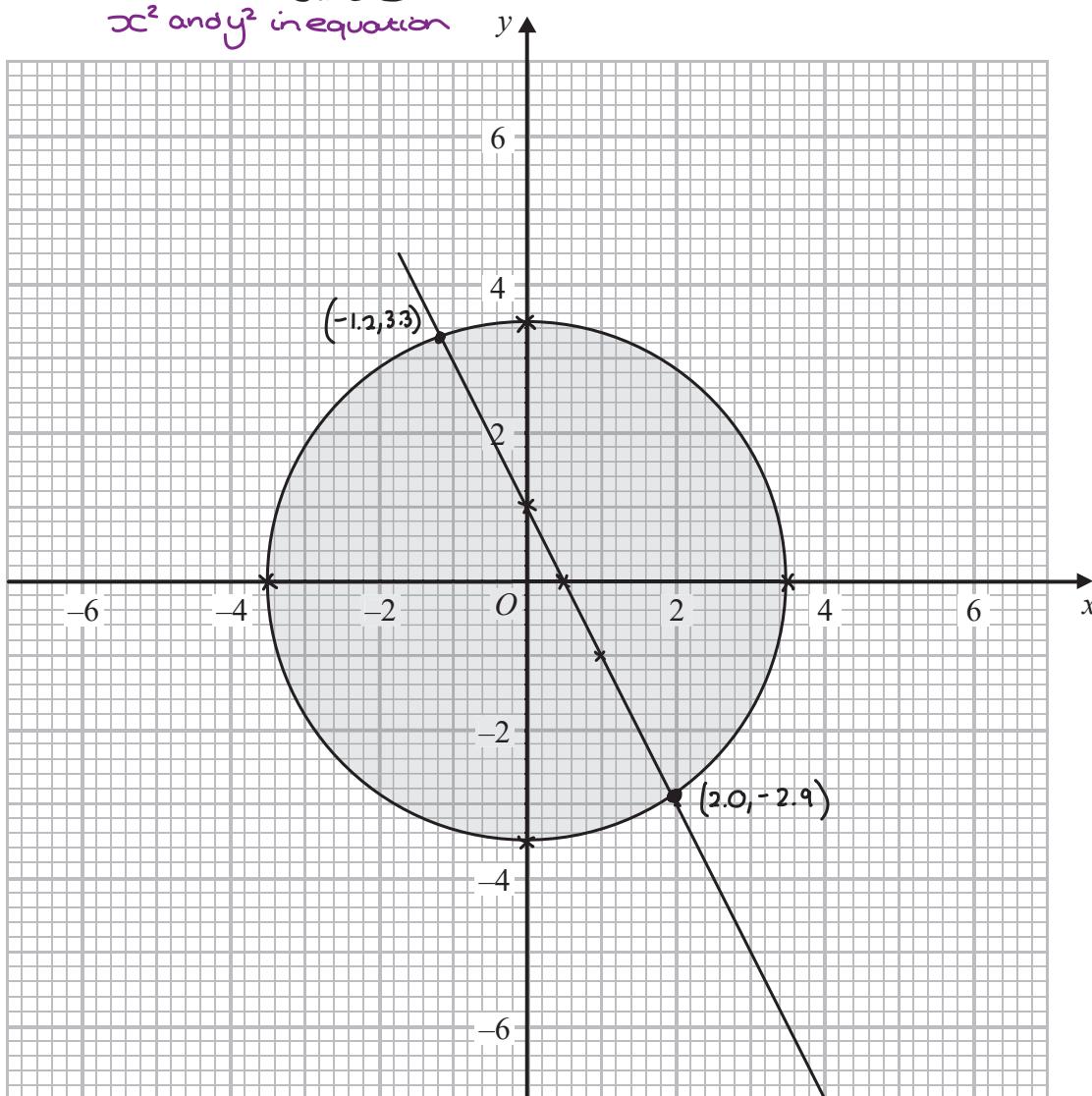
$$y = -2.$$

$$x = \dots \quad -\frac{2}{3}$$

$$y = \dots \quad -2.$$

(Total for Question is 3 marks)

4. (a) On the grid, draw the graph of $x^2 + y^2 = 12.25$ Circle x² and y² in equation radius = $\sqrt{12.25} = 3.5$



(2)

- (b) Hence find estimates for the solutions of the simultaneous equations

$$x^2 + y^2 = 12.25$$

$$2x + y = 1$$

① Draw on grid - find where it meets the circle

① ^{2 correct}

$$x = 2.0 \quad y = -2.9, \quad x = -1.2 \quad y = 3.3$$

(3)

(Total for Question is 5 marks)

5. Solve the simultaneous equations

$$\begin{array}{l} \textcircled{1} \quad 5x + y = 21 \\ \textcircled{2} \quad x - 3y = 9 \end{array}$$

$$\textcircled{1} \times 3$$

$$\begin{array}{rcl} 5x + y & = & 21 \\ \downarrow \times 3 & & \downarrow \times 3 \\ 15x + 3y & = & 63 \end{array}$$

$$\textcircled{3} \quad 15x + 3y = 63$$

$$\textcircled{2} + \textcircled{3}$$

$$\begin{array}{rcl} x - 3y & = & 9 \\ 15x + 3y & = & 63 \\ \hline 16x & = & 72 \end{array}$$

$$\begin{array}{rcl} \downarrow \div 8 & & \downarrow \div 8 \\ 2x & = & 9 \\ \downarrow \div 2 & & \downarrow \div 2 \\ x & = & 4.5 \end{array}$$

$$x - 3y = 9$$

$$\text{When } x = 4.5$$

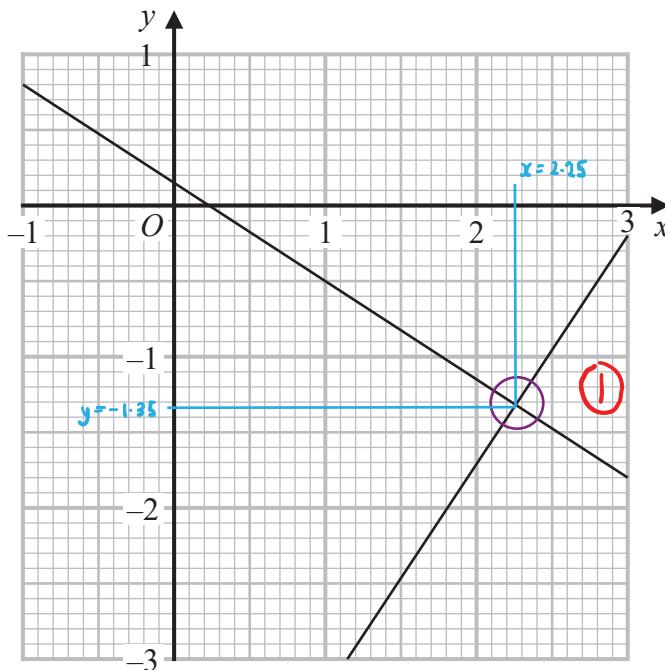
$$\begin{array}{rcl} 4.5 - 3y & = & 9 \\ + 3y & & + 3y \\ \hline 4.5 & = & 9 + 3y \\ - 9 & & - 9 \\ \hline -4.5 & = & 3y \\ \div 3 & & \div 3 \\ -1.5 & = & y \end{array}$$

$$x = \dots \quad 4.5 \dots$$

$$y = \dots \quad -1.5 \quad \checkmark \dots$$

(Total for Question is 3 marks)

6. The graphs with equations $3y + 2x = \frac{1}{2}$ and $2y - 3x = -\frac{113}{12}$ have been drawn on the grid below.



Using the graphs, find estimates of the solutions of the simultaneous equations



$$3y + 2x = \frac{1}{2}$$

solution found at
the point at which
the two lines intersect.

$$2y - 3x = -\frac{113}{12}$$

$$\begin{aligned} x &= 2.25 \\ y &= -1.35 \end{aligned}$$

(Total for Question is 2 marks)

7. Solve algebraically the simultaneous equations

$$\begin{aligned}x^2 - 4y^2 &= 9 \\3x + 4y &= 7\end{aligned}$$

$$\begin{aligned}\textcircled{1} \quad 3x + 4y &= 7 \\3x &= 7 - 4y \\x &= \frac{7 - 4y}{3}\end{aligned}$$

$$\begin{aligned}\textcircled{2} \quad x^2 - 4y^2 &= 9 \\(\frac{7 - 4y}{3})^2 - 4y^2 &= 9 \\49 - 56y + 16y^2 - 4y^2 &\stackrel{=} {\frac{36y^2}{9}}\end{aligned}$$

$$\textcircled{3} \quad \frac{49 - 56y + 16y^2}{9} - \frac{36y^2}{9} = 9 \quad \therefore \frac{49 - 56y + 16y^2 - 36y^2}{9} = 9$$

$$49 - 56y + 16y^2 - 36y^2 = 81. \quad 16y^2 - 36y^2 = -20y^2$$

$$-32 - 56y - 20y^2 = 0 \quad \therefore -20y^2 - 56y - 32 = 0 \quad \text{we can multiply both sides by -1}$$

$$20y^2 + 56y + 32 = 0. \quad \overset{\div 4}{\longrightarrow} \quad 5y^2 + 14y + 8 = 0. \quad \textcircled{1}$$

$$\textcircled{4} \quad 5y^2 + 14y + 8 = 0.$$

$$(5y + 4)(y + 2) = 0$$

$$\therefore y = -2, \quad y = -\frac{4}{5}$$

$$x = \frac{7 - 4y}{3} \quad \textcircled{1}$$

$$\textcircled{5} \quad \text{when } y = -2:$$

$$x = \frac{7 - 4(-2)}{3} = 5. \quad x = 5, \quad y = -2.$$

$$\text{when } y = -\frac{4}{5}:$$

$$x = \frac{7 - 4(-\frac{4}{5})}{3} = \frac{17}{5}. \quad x = \frac{17}{5}, \quad y = -\frac{4}{5}$$

$x = 5, \quad y = -2 \quad \text{and} \quad x = \frac{17}{5}, \quad y = -\frac{4}{5}$

\textcircled{1}

$$x = 5, \quad y = -2 \quad \text{and} \quad x = \frac{17}{5}, \quad y = -\frac{4}{5}$$

(Total for Question is 5 marks)